



WAKE COUNTY
PUBLIC SCHOOL SYSTEM



mathematics
vision project

Transforming Mathematics Education

SECONDARY
MATH TWO

An Integrated Approach

WCPSS Math 2 Unit 5: MVP MODULE 3
**Solving Quadratics &
Other Equations**

MATHEMATICSVISIONPROJECT.ORG

The Mathematics Vision Project

Scott Hendrickson, Joleigh Honey, Barbara Kuehl, Travis Lemon, Janet Sutorius

© 2017 Mathematics Vision Project

Original work © 2013 in partnership with the Utah State Office of Education

This work is licensed under the Creative Commons Attribution CC BY 4.0



MODULE 3 - TABLE OF CONTENTS

Solving Quadratic and Other Equations

3.1 The In-Betweeners – A Develop Understanding Task	Page 1
Examining values of continuous exponential functions between integers (NC.M2.N-RN.1)	
READY, SET, GO Homework: Solving Quadratic & Other Equations 3.1	
3.2 Half-Interested – A Solidify Understanding Task	Page 7
Connecting radicals and rules of exponents to create meaning for rational exponents (NC.M2.N-RN.1)	
READY, SET, GO Homework: Solving Quadratic & Other Equations 3.2	
3.3 More Interesting – A Solidify Understanding Task	Page 15
Verifying that properties of exponents hold true for rational exponents (NC.M2.F-IF.8, NC.M2.N-RN.1, NC.M2.N-RN.2, NC.M2.A-SSE.3)	
READY, SET, GO Homework: Solving Quadratic & Other Equations 3.3	
3.4 Radical Ideas – A Practice Understanding Task	Page 19
Becoming fluent converting between exponential and radical forms of expressions (NC.M2.N-RN.1, NC.M2.N-RN.2)	
READY, SET, GO Homework: Solving Quadratic & Other Equations 3.4	
3.5 Throwing an Interception – A Develop Understanding Task	Page 27
Developing the Quadratic Formula as a way for finding x-intercepts and roots of quadratic functions (NC.M2.A-REI.4a, NC.M1.A-CED.4, NC.M2.F-IF.7)	
READY, SET, GO Homework: Solving Quadratic & Other Equations 3.5	

3.6 Curbside Rivalry – A Solidify Understanding Task

Page 37

Examining how different forms of a quadratic expression can facilitate the solving of quadratic equations

(NC.M2.A-REI.1, NC.M2.A-REI.4, NC.M2.A-CED.1, NC.M2.A-CED.2, NC.M1.A-CED.4)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.6

3.7 Perfecting My Quads – A Solidify Understanding Task

Page 45

Building fluency with solving of quadratic equations

(NC.M2.A-REI.1, NC.M2.A-REI.4a, NC.M2.A-REI.7, NC.M2.A-CED.1, NC.M2.A-CED.2, NC.M1.A.CED.4)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.7

3.8 To Be Determined – A Develop Understanding Task

Page 51

Surfacing the need for complex number as solutions for some quadratic equations

(NC.M2.A-REI.4b)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.8

3.9 My Irrational and Imaginary Friends – A Solidify Understanding Task

Page 57

Extending the real and complex number systems

(NC.M2.N-RN.3, NC.M2.N-CN.1, NC.M2.A-REI.4b)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.9

3.10 iNumbers – A Practice Understanding Task

Page 65

Examining the arithmetic of real and complex numbers (NC.M2.N-RN.3, NC.M2.N-CN.1)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.10

3.11 Quadratic Quandaries – A Develop and Solidify Understanding

Page 73

Task Solving Quadratic Inequalities (NC.M2.A-SSE.1a,b, NC.M2.A-CED.1)

READY, SET, GO Homework: Solving Quadratic & Other Equations 3.11

3.1 The In-Betweeners

A Develop Understanding Task



CC BY Sweet Flour Bake Shop
<https://flic.kr/p/87mQP5>

Now that you've seen that there are contexts for continuous exponential functions, it's a good idea to start thinking about the numbers that fill in between the values like 2^2 and 2^3 in an exponential function. These numbers are actually pretty interesting, so we're going to do some exploring in this task to see what we can find out about these "in-betweeners".

Let's begin in a familiar place:

1. Complete the following table.

x	0	1	2	3	4
$f(x) = 4 \cdot 2^x$	4				

2. Plot these points on the graph at the end of this task, and sketch the graph of $f(x)$.

Let's say we want to create a table with more entries, maybe with a point halfway between each of the points in the table above. There are a couple of ways that we might think about it. We'll begin by letting our friend Travis explain his method.

Travis makes the following claim:

"If the function doubles each time x goes up by 1, then half that growth occurs between 0 and $\frac{1}{2}$ and the other half occurs between $\frac{1}{2}$ and 1. So for example, we can find the output at $x = \frac{1}{2}$ by finding the average of the outputs at $x = 0$ and $x = 1$."

3. Fill in the parts of the table below that you've already computed, and then decide how you might use Travis' strategy to fill in the missing data. Also plot Travis' data on the graph at the end of the task.

x	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2	$\frac{5}{2}$	3	$\frac{7}{2}$	4
$f(x)$	4								

4. Comment on Travis' idea. How does it compare to the table generated in problem 1? For what kind of function would this reasoning work?

Miriam suggests they should fill in the data in the table in the following way:

"I noticed that the function increases by the same factor each time x goes up 1, and I think this is like what we did last year *Geometric Meanies*. To me it seems like this property should hold over each half- interval as well."

5. Fill in the parts of the table below that you've already computed in problem 1, and then decide how you might use Miriam's idea to fill in the missing data. As in the table in problem 1, each entry should be multiplied by some constant factor to get the next entry, and that factor should produce the same results as those already recorded in the table. Use this constant factor to complete the table. Also plot Miriam's data on the graph at the end of this task.

x	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2	$\frac{5}{2}$	3	$\frac{7}{2}$	4
$f(x)$	4								

6. What if Miriam wanted to find values for the function every third of the interval instead of every half? What constant factor would she use to be consistent with the function doubling as x increases by 1. Use this multiplier to complete the following table.

x	0	$\frac{1}{3}$	$\frac{2}{3}$	1	$\frac{4}{3}$	$\frac{5}{3}$	2	$\frac{7}{3}$	$\frac{8}{3}$	3
$f(x)$	4									

7. What number did you use as a constant factor to complete the table in problem 5?
8. What number did you use as a constant factor to complete the table in problem 6?
9. Give a detailed description of how you would estimate the output value $f(x)$, for $x = \frac{5}{3}$.

SECONDARY MATH II // MODULE 3
SOLVING QUADRATIC & OTHER EQUATIONS- 3.1



READY, SET, GO!

Name _____

Period _____

Date _____

READY

Topic: Comparing Additive and Multiplicative Patterns

The sequences below exemplify either an additive (arithmetic) or a multiplicative (geometric) pattern. Identify the type of sequence, fill in the missing values on the table and write an equation.

1.

Term	1st	2nd	3rd	4th	5th	6th	7th	8th
Value	2	4	8	16	32			

a. Type of Sequence:

b. Equation:

2.

Term	1st	2nd	3rd	4th	5th	6th	7th	8th
Value	66	50	34	18				

a. Type of Sequence:

b. Equation:

3.

Term	1st	2nd	3rd	4th	5th	6th	7th	8th
Value	-3	9	-27	81				

a. Type of Sequence:

b. Equation:

4.

Term	1st	2nd	3rd	4th	5th	6th	7th	8th
Value	160	80	40	20				

a. Type of Sequence:

b. Equation:

5.

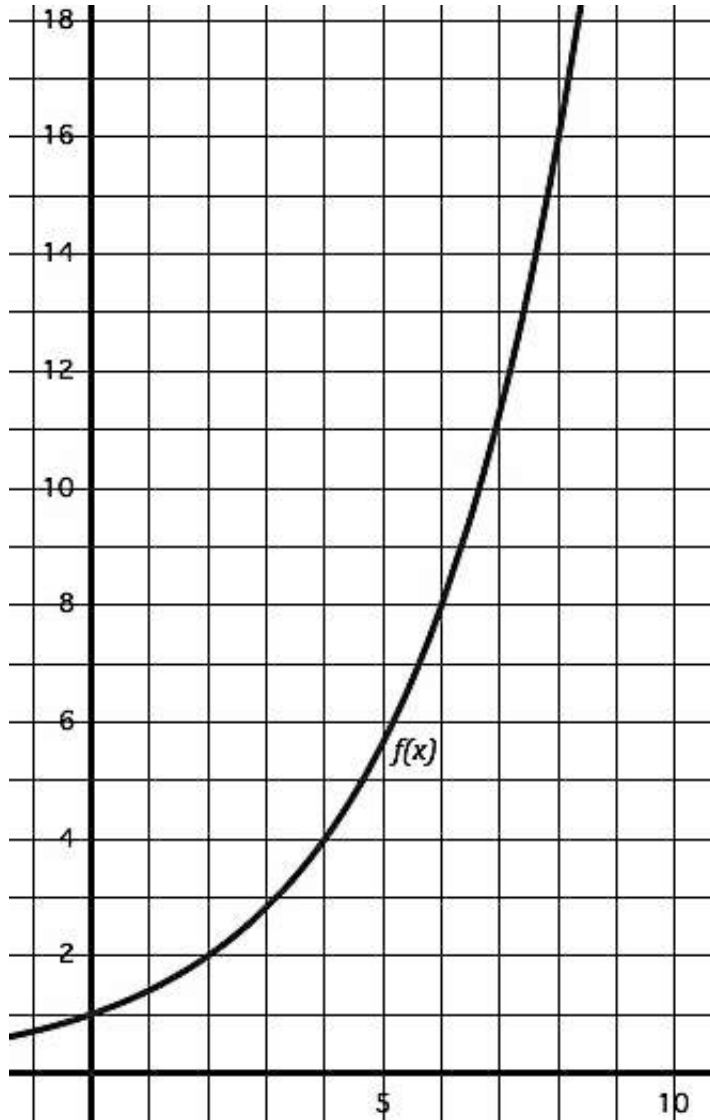
Term	1st	2nd	3rd	4th	5th	6th	7th	8th
Value	-9	-2	5	12				

a. Type of Sequence:

b. Equation:

Need help? Visit www.rsgsupport.org

Use the graph of the function to find the desired values of the function. Also create an explicit equation for the function.



6. Find the value of $f(2)$

7. Find where $f(x) = 4$

8. Find the value of $f(6)$

9. Find where $f(x) = 16$

10. What do you notice about the way that inputs and outputs for this function relate?
(Create an in-out table if you need to.)

11. What is the explicit equation for this function?

Need help? Visit www.rsgsupport.org

SET

Topic: Evaluate the Expressions with Rational Exponents

Fill in the missing values of the table based on the growth that is described.

12. The growth in the table is triple at each whole year.

Years	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2	$\frac{5}{2}$	3	$\frac{7}{2}$	4
bacteria	2		6						

13. The growth in the table is triple at each whole year.

Years	0	$\frac{1}{3}$	$\frac{2}{3}$	1	$\frac{4}{3}$	$\frac{5}{3}$	2	$\frac{7}{3}$	$\frac{8}{3}$
bacteria	2			6					

14. The values in the table grow by a factor of four at each whole year.

Years	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2	$\frac{5}{2}$	3	$\frac{7}{2}$	4
bacteria	2		8						

GO

Topic: Simplifying Exponents

Simplify the following expressions using exponent rules and relationships, write your answers in exponential form. (For example: $2^2 \cdot 2^5 = 2^7$)

15. $3^2 \cdot 3^5$

16. $\frac{5^3}{5^2}$

17. 2^{-5}

18. 17^0

19. $\frac{7^5}{7^2} \cdot \frac{7^3}{7^4}$

20. $\frac{3^{-2} \cdot 3^5}{3^7}$

Need help? Visit www.rsgsupport.org



CC BY TaxCredits.net
<https://flic.kr/p/chEwR9>

3.2 Half Interested

A Solidify Understanding Task

Carlos and Clarita, the Martinez twins, have run a summer business every year for the past five years. Their first business, a neighborhood lemonade stand, earned a small profit that their father insisted they deposit in a savings account at the local bank. When the Martinez family moved a few months later, the twins decided to leave the money in the bank where it has been earning 5% interest annually. Carlos was reminded of the money when he found the annual bank statement they had received in the mail.

“Remember how Dad said we could withdraw this money from the bank when we are twenty years old,” Carlos said to Clarita. “We have \$382.88 in the account now. I wonder how much that will be five years from now?”

1. Given the facts listed above, how can the twins figure out how much the account will be worth five years from now when they are twenty years old? Describe your strategy and calculate the account balance.
2. Carlos calculates the value of the account one year at a time. He has just finished calculating the value of the account for the first four years. Describe how he can find the next year’s balance, and record that value in the table.

year	amount
0	382.88
1	402.02
2	422.12
3	443.23
4	465.39
5	

3. Clarita thinks Carlos is silly calculating the value of the account one year at a time, and says that he could have written a formula for the n^{th} year and then evaluated his formula when $n = 5$. Write Clarita’s formula for the n^{th} year and use it to find the account balance at the end of year 5.

4. Carlos was surprised that Clarita’s formula gave the same account balance as his year-by-year strategy. Explain, in a way that would convince Carlos, why this is so.

“I can’t remember how much money we earned that summer,” said Carlos. “I wonder if we can figure out how much we deposited in the account five years ago, knowing the account balance now?”

5. Carlos continued to use his strategy to extend his table year-by-year back five years. Explain what you think Carlos is doing to find his table values one year at a time, and continue filling in the table until you get to -5, which Carlos uses to represent “five years ago”.

year	amount
-5	
-4	
-3	
-2	
-1	364.65
0	382.88
1	402.02
2	422.12
3	443.23
4	465.39
5	

6. Clarita evaluated her formula for $n = -5$. Again Carlos is surprised that they get the same results. Explain why Clarita’s method works.

Clarita doesn’t think leaving the money in the bank for another five years is such a great idea, and suggests that they invest the money in their next summer business, *Curbside Rivalry* (which, for now, they are keeping top secret from everyone, including their friends). “We’ll have some start up costs, and this will pay for them without having to withdraw money from our other accounts.”

Carlos remarked, "But we'll be withdrawing our money halfway through the year. Do you think we'll lose out on this year's interest?"

"No, they'll pay us a half-year portion of our interest," replied Clarita.

"But how much will that be?" asked Carlos.

7. Calculate the account balance and how much interest you think Carlos and Clarita should be paid if they withdraw their money $\frac{1}{2}$ year from now. Remember that they currently have \$382.88 in the account, and that they earn 5% annually. Describe your strategy.

Carlos used the following strategy: He calculated how much interest they should be paid for a full year, found half of that, and added that amount to the current account balance.

Clarita used this strategy: She substituted $\frac{1}{2}$ for n in the formula $A = 382.88(1.05)^n$ and recorded this as the account balance.

8. This time Carlos and Clarita didn't get the same result. Whose method do you agree with and why?

Clarita is trying to convince Carlos that her method is correct. "Exponential rules are multiplicative, not additive. Look back at your table. We will earn \$82.51 in interest during the next four years. If your method works we should be able to take half of that amount, add it to the amount we have now, and get the account balance we should have in two years, but it isn't the same."

9. Carry out the computations that Clarita suggested and compare the result for year 2 using this strategy as opposed to the strategy Carlos originally used to fill out the table.

10. The points from Carlos' table (see question 2) have been plotted on the graph at the end of this task, along with Clarita's function. Plot the value you calculated in question 9 on this same graph. What does the graph reveal about the differences in Carlos' two strategies?

11. Now plot Clarita's and Carlos' values for $\frac{1}{2}$ year (see question 8) on this same graph.

"Your data point seems to fit the shape of the graph better than mine," Carlos conceded, "but I don't understand how we can use $\frac{1}{2}$ as an exponent. How does that find the correct factor we need to multiply by? In your formula, writing $(1.05)^5$ means multiply by 1.05 five times, and writing $(1.05)^{-5}$ means divide by 1.05 five times, but what does $(1.05)^{\frac{1}{2}}$ mean?"

Clarita wasn't quite sure how to answer Carlos' question, but she had some questions of her own. She decided to jot them down, including Carlos' question:

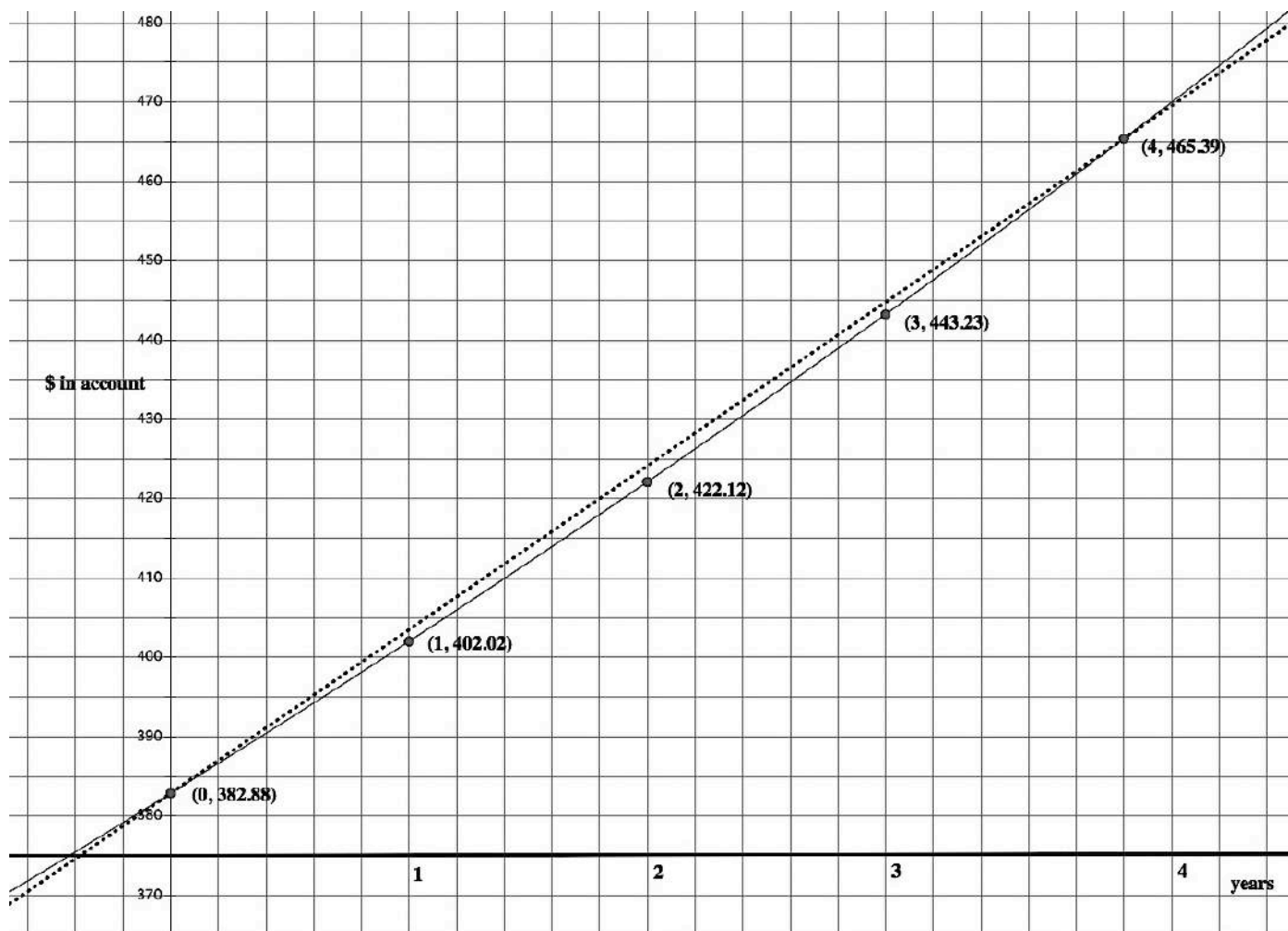
- What numerical amount do we multiply by when we use $(1.05)^{\frac{1}{2}}$ as a factor?
- What happens if we multiply by $(1.05)^{\frac{1}{2}}$ and then multiply the result by $(1.05)^{\frac{1}{2}}$ again? Shouldn't that be a full year's worth of interest? Is it?
- If multiplying by $(1.05)^{\frac{1}{2}} \cdot (1.05)^{\frac{1}{2}}$ is the same as multiplying by 1.05, what does that suggest about the value of $(1.05)^{\frac{1}{2}}$?

12. Answer each of Clarita's questions listed above as best as you can.

As Carlos is reflecting on this work, Clarita notices the date on the bank statement that started this whole conversation. “This bank statement is three months old!” she exclaims. “That means the bank will owe us $\frac{3}{4}$ of a year’s interest.”

“So how much interest will the bank owe us then?” asked Carlos.

13. Find as many ways as you can to answer Carlos’ question: How much will their account be worth in $\frac{3}{4}$ of a year (nine months) if it earns 5% annually and is currently worth \$382.88?



READY, SET, GO!

Name _____

Period _____

Date _____

READY

Topic: Simplifying Radicals

A very common radical expression is a square root. One way to think of a square root is the number that will multiply by itself to create a desired value. For example: $\sqrt{2}$ is the number that will multiply by itself to equal 2. And in like manner $\sqrt{16}$ is the number that will multiply by itself to equal 16, in this case the value is 4 because $4 \times 4 = 16$. (When the square root of a square number is taken you get a nice whole number value. Otherwise an irrational number is produced.)

This same pattern holds true for other radicals such as cube roots and fourth roots and so forth. For example: $\sqrt[3]{8}$ is the number that will multiply by itself three times to equal 8. In this case it is equal to the value of 2 because $2^3 = 2 \times 2 \times 2 = 8$.

With this in mind radicals can be simplified. See the examples below.

<p>Example 1: Simplify $\sqrt{20}$</p> $\sqrt{20} = \sqrt{4 \cdot 5} = \sqrt{2 \cdot 2 \cdot 5} = 2\sqrt{5}$	<p>Example 2: Simplify $\sqrt[5]{96}$</p> $\sqrt[5]{96} = \sqrt[5]{2^5 \cdot 3} = 2\sqrt[5]{3}$
---	--

Simplify each of the radicals.

1. $\sqrt{40}$

2. $\sqrt{50}$

3. $\sqrt[3]{16}$

4. $\sqrt{72}$

5. $\sqrt[4]{81}$

6. $\sqrt{32}$

7. $\sqrt[5]{160}$

8. $\sqrt{45}$

9. $\sqrt[3]{54}$

Need help? Visit www.rsgsupport.org

SET

Topic: Finding arithmetic and geometric means and making meaning of rational exponents
 You may have found arithmetic and geometric means in your prior work. Finding arithmetic and geometric means requires finding values of a sequence between given values from non-consecutive terms. In each of the sequences below determine the means and show how you found them.

Find the **arithmetic** means for the following. Show your work.

10.

x	1	2	3
y	5		11

11.

x	1	2	3	4	5
y	18				-10

12.

x	1	2	3	4	5	6	7
y	12						-6

Find the **geometric** means for the following. Show your work.

13.

x	1	2	3
y	3		12

14.

x	1	2	3	4
y	7			875

15.

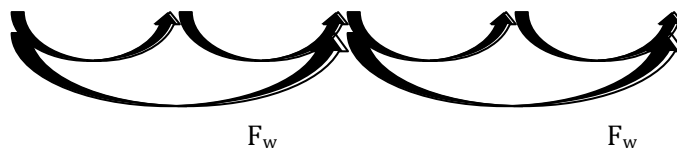
x	1	2	3	4	5	6
y	4					972

Fill in the tables of values and find the factor used to move between whole number values, F_w , as well as the factor, F_c , used to move between each column of the table.

16.

x	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2
y	4		16		

d. $F_w =$
 e. $F_c =$

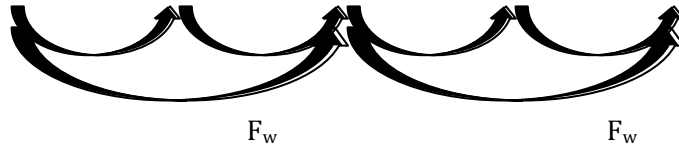


Need help? Visit www.rsgsupport.org

17.

x	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2
y	4		8		

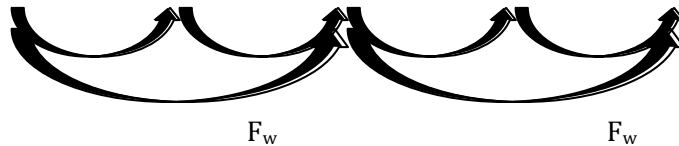
d. $F_w =$
 e. $F_c =$



18.

x	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2
y	5		15		

d. $F_w =$
 e. $F_c =$



GO

Topic: Simplifying Exponents

Find the desired values for each function below.

19. $f(x) = 2x - 7$

Find $f(-3)$

Find $f(x) = 21$

Find $f\left(\frac{1}{2}\right)$

20. $g(x) = 3^x(2)$

Find $g(-4)$

Find $g(x) = 162$

Find $g\left(\frac{1}{2}\right)$

21. $I(t) = 210(1.08^t)$

Find $I(12)$

Find $I(t) = 420$

Find $I\left(\frac{1}{2}\right)$

22. $h(x) = x^2 + x - 6$

Find $h(-5)$

Find $h(x) = 0$

Find $h\left(\frac{1}{2}\right)$

23. $k(x) = -5x + 9$

Find $k(-7)$

Find $k(x) = 0$

Find $k\left(\frac{1}{2}\right)$

24. $m(x) = (5^x)2$

Find $m(-2)$

Find $m(x) = 1$

Find $m\left(\frac{1}{2}\right)$

Need help? Visit www.rsgsupport.org



CC BY Pictures of Money
<https://pic.kr/b/s684tk>

3.3 More Interesting

A Solidify Understanding Task

Carlos now knows he can calculate the amount of interest earned on an account in smaller increments than one full year. He would like to determine how much money is in an account each month that earns 5% annually with an initial deposit of \$300.

He starts by considering the amount in the account each month during the first year. He knows that by the end of the year the account balance should be \$315, since it increases 5% during the year.

1. Complete the table showing what amount is in the account each month during the first twelve months.

Time	0													1 year
Account balance	\$300													\$315

2. What number did you multiply the account by each month to get the next month's balance?

Carlos knows the exponential equation that gives the account balance for this account on an annual basis is $A = 300(1.05)^t$. Based on his work finding the account balance each month, Carlos writes the following equation for the same account: $A = 300(1.05^{1/12})^{12t}$.

3. Verify that both equations give the same results. Using the properties of exponents, explain why these two equations are equivalent.
4. What is the meaning of the $12t$ in this equation?

Carlos shows his equation to Clarita. She suggests his equation could also be approximated by $A = 300(1.004)^{12t}$, since $(1.05)^{\frac{1}{12}} \approx 1.004$. Carlos replies, "I know the 1.05 in the equation $A = 300(1.05)^t$ means I am earning 5% interest annually, but what does the 1.004 mean in your equation?"

5. Answer Carlos' question. What does the 1.004 mean in $A = 300(1.004)^{12t}$?

The properties of exponents can be used to explain why $[(1.05)^{\frac{1}{12}}]^{12t} = 1.05^t$. Here are some more examples of using the properties of exponents with rational exponents. For each of the following, simplify the expression using the properties of exponents, and explain what the expression means in terms of the context.

6. $(1.05)^{\frac{1}{12}} \cdot (1.05)^{\frac{1}{12}} \cdot (1.05)^{\frac{1}{12}}$

7. $[(1.05)^{\frac{1}{12}}]^6$

8. $(1.05)^{-\frac{1}{12}}$

9. $(1.05)^2 \cdot (1.05)^{\frac{1}{4}}$

10. $\frac{(1.05)^2}{(1.05)^{\frac{1}{2}}}$

11. Use $\left[(1.05)^{\frac{1}{12}} \right]^{12} = 1.05$ to explain why $(1.05)^{\frac{1}{12}} = \sqrt[12]{1.05}$

READY, SET, GO!

Name

Period

Date

READY

Topic: Meaning of Exponents

In the table below there is a column for the exponential form, the meaning of that form, which is a list of factors and the standard form of the number. Fill in the form that is missing.

Exponential form	List of factors	Standard Form
5^3	$5 \cdot 5 \cdot 5$	125
1a.	$7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7$	b.
2. 2^{10}	a.	b.
3a.	b.	81
4. 11^5	a.	b.
5a.	$3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3$	b.
6a.	b.	625

Provide at least three other equivalent forms of the exponential expression. Use rules of exponents such as $3^5 \cdot 3^6 = 3^{11}$ and $(5^2)^3 = 5^6$ as well as division properties and others.

	1 st Equivalent Form	Equivalent Form	Equivalent Form
7. $2^{10} =$			
8. $3^7 =$			
9. $13^{-8} =$			
10. $7^{\frac{1}{3}} =$			
11. $5^1 =$			

Need help? Visit www.rsgsupport.org

SET

Topic: Finding equivalent expressions and functions

Determine whether all three expressions in each problem below are equivalent. Justify why or why they are not equivalent.

12.	$5(3^{x-1})$	$15(3^{x-2})$	$\frac{5}{3}(3^x)$
13.	$64(2^{-x})$	$\frac{64}{2^x}$	$64\left(\frac{1}{2}\right)^x$
14.	$3(x-1)+4$	$3x - 1$	$3(x-2) + 7$
15.	$50(2^{x+2})$	$25(2^{2x+1})$	$50(4^x)$
16.	$30(1.05^x)$	$30\left(1.05^{\frac{1}{7}}\right)^{7x}$	$30\left(1.05^{\frac{x}{2}}\right)^2$
17.	$20(1.1^x)$	$20(1.1^{-1})^{-1x}$	$20\left(1.1^{\frac{1}{5}}\right)^{5x}$

GO

Topic: Using rules of exponents

Simplify each expression. Your answer should still be in exponential form.

18.	$7^3 \cdot 7^5 \cdot 7^2$	19.	$(3^4)^5$	20.	$(5^3)^4 \cdot 5^7$
21.	$x^3 \cdot x^5$	22.	x^{-b}	23.	$x^a \cdot x^b$
24.	$(x^a)^b$	25.	$\frac{y^a}{y^b}$	26.	$\frac{(y^a)^c}{y^b}$
27.	$\frac{(3^4)^6}{3^7}$	28.	$\frac{r^5s^3}{rs^2}$	29.	$\frac{x^5y^{12}z^0}{x^8y^9}$

Need help? Visit www.rsgsupport.org



3.4 Radical Ideas

A Practice Understanding Task

Now that Tia and Tehani know that $a^{m/n} = (\sqrt[n]{a})^m$ they are wondering which form, radical form or exponential form, is best to use when working with numerical and algebraic expressions.

Tia says she prefers radicals since she understands the following properties for radicals (and there are not too many properties to remember):

If n is a positive integer greater than 1 and both a and b are positive real numbers then,

1. $\sqrt[n]{a^n} = a$
2. $\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b}$
3. $\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$

Tehania says she prefers exponents since she understands the following properties for exponents (and there are more properties to work with):

1. $a^m \cdot a^n = a^{m+n}$
2. $(a^m)^n = a^{mn}$
3. $(ab)^n = a^n \cdot b^n$
4. $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$
5. $\frac{a^m}{a^n} = a^{m-n}, a \neq 0$
6. $a^{-n} = \frac{1}{a^n}$

DO THIS: Illustrate with examples and explain, using the properties of radicals and exponents, why $a^{1/n} = \sqrt[n]{a}$ and $a^{m/n} = (\sqrt[n]{a})^m$ are true identities.

Using their preferred notation, Tia might simplify $\sqrt[3]{x^8}$ as follows:

$$\sqrt[3]{x^8} = \sqrt[3]{x^3 \cdot x^3 \cdot x^2} = \sqrt[3]{x^3} \cdot \sqrt[3]{x^3} \cdot \sqrt[3]{x^2} = x \cdot x \cdot \sqrt[3]{x^2} = x^2 \cdot \sqrt[3]{x^2}$$

(Tehani points out that Tia also used some exponent rules in her work.)

On the other hand, Tehani might simplify $\sqrt[3]{x^8}$ as follows:

$$\sqrt[3]{x^8} = x^{8/3} = x^{2+2/3} = x^2 \cdot x^{2/3} \text{ or } x^2 \cdot \sqrt[3]{x^2}$$

For each of the following problems, simplify the expression in the ways you think Tia and Tehani might do it.

Original expression	What Tia and Tehani might do to simplify the expression:
$\sqrt{27}$	Tia's method
	Tehani's method
$\sqrt[3]{32}$	Tia's method
	Tehani's method

$\sqrt{20x^7}$	Tia's method
	Tehani's method
$\sqrt[3]{\frac{16xy^5}{x^7y^2}}$	Tia's method
	Tehani's method

Tia and Tehani continue to use their preferred notation when solving equations.

For example, Tia might solve the equation $(x + 4)^3 = 27$ as follows:

$$\begin{aligned} (x + 4)^3 &= 27 \\ \sqrt[3]{(x + 4)^3} &= \sqrt[3]{27} = \sqrt[3]{3^3} \\ x + 4 &= 3 \\ x &= -1 \end{aligned}$$

Tehani might solve the same equation as follows:

$$\begin{aligned} (x + 4)^3 &= 27 \\ \left[(x + 4)^3 \right]^{1/3} &= 27^{1/3} = (3^3)^{1/3} \\ x + 4 &= 3 \\ x &= -1 \end{aligned}$$

For each of the following problems, simplify the expression in the ways you think Tia and Tehani might do it.

Original equation	What Tia and Tehani might do to solve the equation:
$(x - 2)^2 = 50$	Tia's method
	Tehani's method
$9(x - 3)^2 = 4$	Tia's method
	Tehani's method

Zac is showing off his new graphing calculator to Tia and Tehani. He is particularly excited about how his calculator will help him visualize the solutions to equations.

“Look,” Zac says. “I treat the equation like a system of two equations. I set the expression on the left equal to y_1 and the expression of the right equal to y_2 , and I know at the x value where the graphs intersect the expressions are equal to each other.”

Zac shows off his new method on both of the equations Tia and Tehani solved using the properties of radicals and exponents. To everyone's surprise, both equations have a second solution.

1. Use Zac's graphical method to show that both of these equations have two solutions. Determine the exact values of the solutions you find on the calculator that Tia and Tehani did not find using their algebraic methods.

Tia and Tehani are surprised when they realize that both of these equations have more than one answer.

2. Explain why there is a second solution to each of these problems.
3. Modify Tia's and Tehani's algebraic approaches so they will find both solutions.

READY, SET, GO!

Name

Period

Date

READY

Topic: Standard form or Quadratic form

In each of the quadratic equations, $ax^2 + bx + c = 0$ identify the values of a, b and c.

1. $x^2 + 3x + 2 = 0$

a =

b =

c =

2. $2x^2 + 3x + 1 = 0$

a =

b =

c =

3. $x^2 - 4x - 12 = 0$

a =

b =

c =

Write each of the quadratic expressions in factored form.

4. $x^2 + 3x + 2$

5. $2x^2 + 3x + 1$

6. $x^2 - 4x - 12$

7. $x^2 - 3x + 2$

8. $x^2 - 5x - 6$

9. $x^2 - 4x + 4$

10. $x^2 + 8x - 20$

11. $x^2 + x - 12$

12. $x^2 - 7x + 12$

Need help? Visit www.rsgsupport.org

Mathematics Vision Project

Licensed under the Creative Commons Attribution CC BY 4.0

mathematicsvisionproject.org



SET

Topic: Radical notation and radical exponents

Each of the expressions below can be written using either radical notation, $\sqrt[n]{a^m}$ or rational exponents $a^{\frac{m}{n}}$. Rewrite each of the given expressions in the form that is missing. Express in most simplified form.

	<u>Radical Form</u>	<u>Exponential Form</u>
13.	$\sqrt[3]{5^2}$	
14.		$16^{\frac{3}{4}}$
15.	$\sqrt[3]{5^7 \cdot 3^5}$	
16.		$9^{\frac{2}{3}} \cdot 9^{\frac{4}{3}}$
17.	$\sqrt[5]{x^{13}y^{21}}$	
18.	$\sqrt[3]{27a^5b^2}$	
19.	$\sqrt[5]{\frac{32x^{13}}{243y^{15}}}$	
20.		$9^{\frac{3}{2}}s^{\frac{6}{3}}t^{\frac{1}{2}}$

Solve the equations below, use radicals or rational exponents as needed.

21. $(x + 5)^4 = 81$

22. $2(x - 7)^5 + 3 = 67$

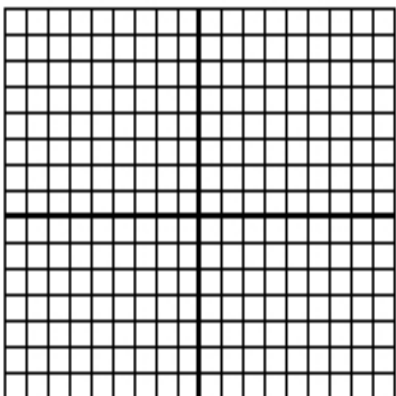
Need help? Visit www.rsgsupport.org

GO

Topic: x-intercepts and y-intercepts for linear, exponential and quadratic functions

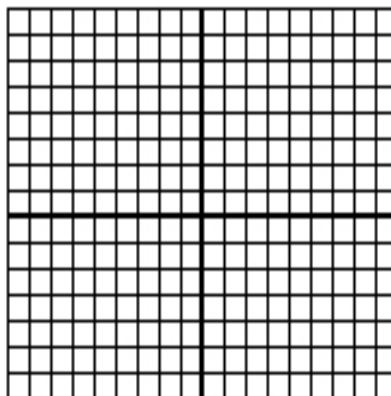
Given the function, find the x-intercept (s) and y-intercept if they exist and then use them to graph a sketch of the function.

23. $f(x) = (x + 5)(x - 4)$



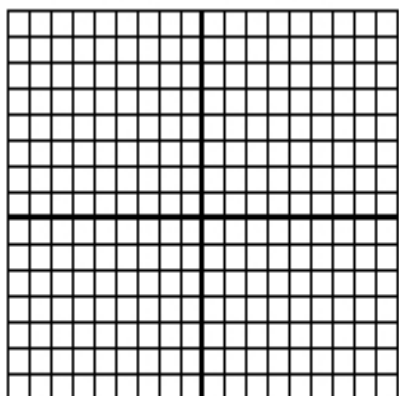
a. x-intercept(s): b. y-intercept:

24. $g(x) = 5(2^{x-1})$



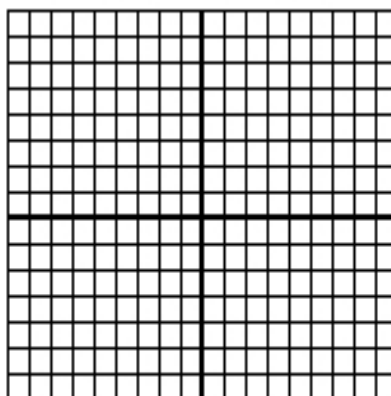
a. x-intercept(s): b. y-intercept:

25. $h(x) = -2(x + 3)$



a. x-intercept(s): b. y-intercept:

26. $k(x) = x^2 - 4$



a. x-intercept(s): b. y-intercept:

Need help? Visit www.rsgsupport.org



CC BY Paul L Dineen
<https://flic.kr/p/aA4RwK>

3.5 Throwing an Interception

A Develop Understanding Task

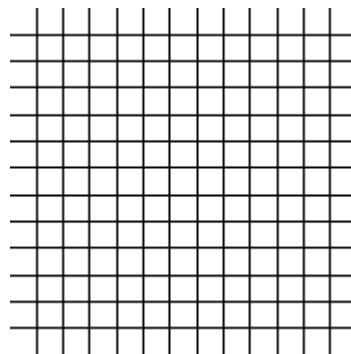
The x -intercept(s) of the graph of a function $f(x)$ are often very important because they are the solution to the equation $f(x) = 0$. In past tasks, we learned how to find the x -intercepts of the function by factoring, which works great for some functions, but not for others. In this task we are going to work on a process to find the x -intercepts of any quadratic function that has them. We'll start by thinking about what we already know about a few specific quadratic functions and then use what we know to generalize to all quadratic functions with x -intercepts.

1. What can you say about the graph of the function $f(x) = x^2 - 2x - 3$?

a. Graph the function

b. What is the equation of the line of symmetry?

c. What is the vertex of the function?



2. Now let's think specifically about the x -intercepts.

a. What are the x -intercepts of $f(x) = x^2 - 2x - 3$?

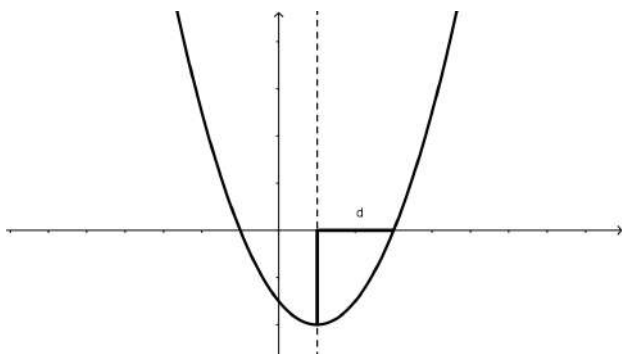
b. How far are the x -intercepts from the line of symmetry?

c. If you knew the line of symmetry was the line $x = h$, and you know how far the x -intercepts are from the line of symmetry, how would you find the actual x -intercepts?

d. How far above the vertex are the x -intercepts?

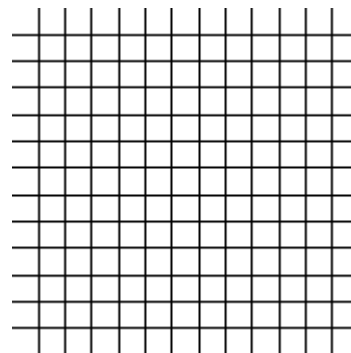
e. What is the value of $f(x)$ at the x -intercepts?

Just to make it a little easier to talk about some of the features that relate to the intercepts, let's name them with variables. From now on, when we talk about the distance from the line of symmetry to either of the x intercepts, we'll call it d . The diagram below shows this feature.



We will always refer to the line of symmetry as the line $x = h$, so the two x-intercepts will be at the points $(h - d, 0)$ and $(h + d, 0)$.

3. So, let's think about another function: $f(x) = x^2 - 6x + 4$
- Graph the function by putting the equation into vertex form.



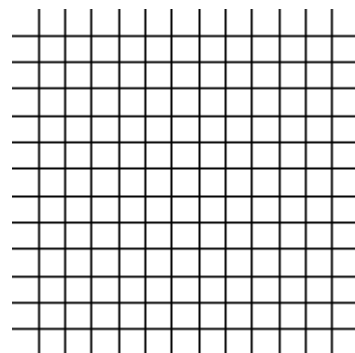
- What is the vertex of the function?
- What is the equation of the line of symmetry?
- What do you estimate the x-intercepts of the function to be?
- What do you estimate d to be?
- What is the value of $f(x)$ at the x-intercepts?

- g. Using the vertex form of the equation and your answer to part “f” above, write an equation and solve it to find the exact values of the x intercepts.

 - h. What is the exact value of d ?

 - i. Use a calculator to find approximations for the x -intercepts. How do they compare with your estimates?
4. What about a function with a vertical stretch? Can we find exact values for the x -intercepts the same way? Let’s try it with: $f(x) = 2x^2 - 8x + 5$.

a. Graph the function by putting the equation into vertex form.



- b. What is the vertex of the function?

- c. What is the equation of the line of symmetry?

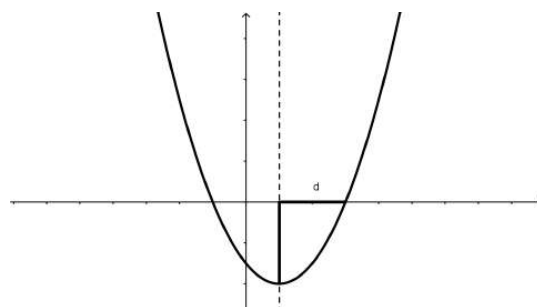
- d. What do you estimate the x -intercepts of the function to be?

- e. What do you estimate d to be?

- f. What is the value of $f(x)$ at the x -intercepts?

- g. Using the vertex form of the equation and your answer to “f” above, write an equation and solve it to find the exact values of the x -intercepts.
- h. What is the exact value of d ?
- i. Compare your solution to your estimate of the roots. How did you do?

5. Finally, let's try to generalize this process by using:
 $f(x) = ax^2 + bx + c$ to represent any quadratic function that has x -intercepts. Here's a possible graph of $f(x)$.



- a. Start the process the usual way by putting the equation into vertex form. It's a little tricky, but just do the same thing with a , b , and c as what you did in the last problem with the numbers.
- b. What is the vertex of the parabola?

- c. What is the line of symmetry of the parabola?
- d. Write and solve the equation for the x -intercepts just as you did previously.
6. How could you use the solutions you just found to tell what the x -intercepts are for the function $f(x) = x^2 - 3x - 1$?
7. You may have found the algebra for writing the general quadratic function $f(x) = ax^2 + bx + c$ in vertex form a bit difficult. Here is another way we can work with the general quadratic function leading to the same results you should have arrived at in 5d.
- a. Since the two x -intercepts are d units from the line of symmetry $x = h$, if the quadratic crosses the x -axis its x -intercepts are at $(h - d, 0)$ and $(h + d, 0)$. We can always write the factored form of a quadratic if we know its x -intercepts. The factored form will look like $f(x) = a(x - p)(x - q)$ where p and q are the two x -intercepts. So, using this information, write the factored form of the general quadratic $f(x) = ax^2 + bx + c$ using the fact that its x -intercepts are at $h-d$ and $h+d$.
- b. Multiply out the factored form (you will be multiplying two **trinomial** expressions together) to get the quadratic in standard form. Simplify your result as much as possible by combining like terms.

- c. You now have the same general quadratic function written in standard form in two different ways, one where the **coefficients** of the terms are a , b and c and one where the coefficients of the terms are expressions involving a , h and d . Match up the coefficients; that is, b , the coefficient of x in one version of the standard form is equivalent to _____ in the other version of the standard form. Likewise c , the constant term in one version of the standard form is equivalent to _____ in the other.
- d. Solve the equations $b = \underline{\hspace{2cm}}$ and $c = \underline{\hspace{2cm}}$ for h and d . Work with your equations until you can express h and d with expressions that only involve a , b and c .
- e. Based on this work, how can you find the x -intercepts of any quadratic using only the values for a , b and c ?
- f. How does your answer to “e” compare to your result in 5d?
8. All of the functions that we have worked with on this task have had graphs that open upward. Would the formula work for parabolas that open downward? Tell why or why not using an example that you create using your own values for the coefficients a , b , and c .

READY, SET, GO!

Name _____

Period _____

Date _____

READY

Topic: Converting measurement of area, area and perimeter.

While working with areas is sometimes essential to convert between units of measure, for example changing from square yards to square feet and so forth. Convert the areas below to the desired measure. (Hint: area is two dimensional, for example $1 \text{ yd}^2 = 9 \text{ ft}^2$ because 3 ft along each side of a square yard equals 9 square feet.)

- | | | |
|---------------------------------------|--|--|
| 1. $7 \text{ yd}^2 = ? \text{ ft}^2$ | 2. $5 \text{ ft}^2 = ? \text{ in}^2$ | 3. $1 \text{ mile}^2 = ? \text{ ft}^2$ |
| 4. $100 \text{ m}^2 = ? \text{ cm}^2$ | 5. $300 \text{ ft}^2 = ? \text{ yd}^2$ | 6. $96 \text{ in}^2 = ? \text{ ft}^2$ |

SET

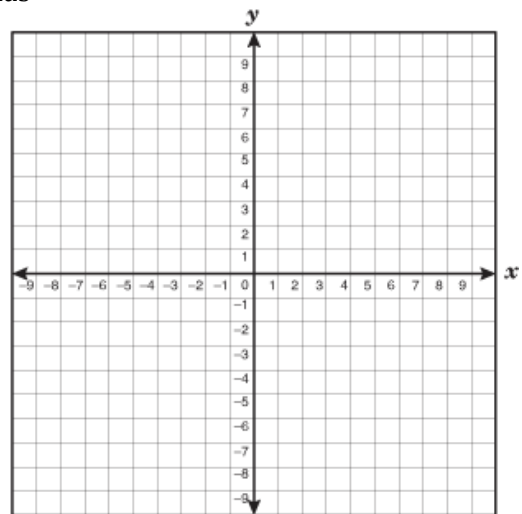
Topic: Transformations and parabolas, symmetry and parabolas

7a. Graph each of the quadratic functions.

$$f(x) = x^2$$

$$g(x) = x^2 - 9$$

$$h(x) = (x + 2)^2 - 9$$



- b. How do the functions compare to each other?
- c. How do $g(x)$ and $h(x)$ compare to $f(x)$?
- d. Look back at the functions above and identify the x-intercepts of $g(x)$. What are they?
- e. What are the coordinates of the points corresponding to the x-intercepts in $g(x)$ in each of the other functions? How do these coordinates compare to one another?

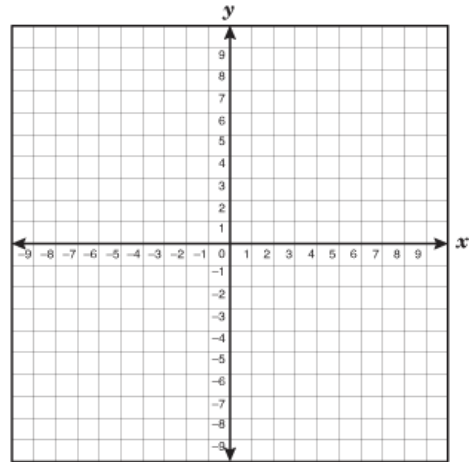
Need help? Visit www.rsgsupport.org

8a. Graph each of the quadratic functions.

$$f(x) = x^2$$

$$g(x) = x^2 - 4$$

$$h(x) = (x - 1)^2 - 4$$



b. How do the functions compare to each other?

c. How do $g(x)$ and $h(x)$ compare to $f(x)$?

d. Look back at the functions above and identify the x-intercepts of $g(x)$. What are they?

e. What are the coordinates of the points corresponding to the x-intercepts in $g(x)$ in each of the other functions? How do these coordinates compare to one another?

9. How can the transformations that occur to the function $f(x) = x^2$ be used to determine where the x-intercepts of the function's image will be?

GO

Topic: Function Notation and Evaluating Functions

Use the given functions to find the missing values. (Check your work using a graph.)

10. $f(x) = x^2 + 4x - 12$

a. $f(0) = \underline{\hspace{2cm}}$

b. $f(2) = \underline{\hspace{2cm}}$

c. $f(x) = 0, \quad x = \underline{\hspace{2cm}}$

d. $f(x) = 20, \quad x = \underline{\hspace{2cm}}$

11. $g(x) = (x - 5)^2 + 2$

a. $g(0) = \underline{\hspace{2cm}}$

b. $g(5) = \underline{\hspace{2cm}}$

c. $g(x) = 0, \quad x = \underline{\hspace{2cm}}$

d. $g(x) = 16, \quad x = \underline{\hspace{2cm}}$

Need help? Visit www.rsgsupport.org

12. $f(x) = x^2 - 6x + 9$

a. $f(0) = \underline{\hspace{2cm}}$

b. $f(-3) = \underline{\hspace{2cm}}$

c. $f(x) = 0, x = \underline{\hspace{2cm}}$

d. $f(x) = 16, x = \underline{\hspace{2cm}}$

13. $g(x) = (x - 2)^2 - 3$

a. $g(0) = \underline{\hspace{2cm}}$

b. $g(5) = \underline{\hspace{2cm}}$

c. $g(x) = 0, x = \underline{\hspace{2cm}}$

d. $g(x) = -3, x = \underline{\hspace{2cm}}$

14. $f(x) = (x + 5)^2$

a. $f(0) = \underline{\hspace{2cm}}$

b. $f(-2) = \underline{\hspace{2cm}}$

c. $f(x) = 0, x = \underline{\hspace{2cm}}$

d. $f(x) = 9, x = \underline{\hspace{2cm}}$

15. $g(x) = -(x + 1)^2 + 8$

a. $g(0) = \underline{\hspace{2cm}}$

b. $g(2) = \underline{\hspace{2cm}}$

c. $g(x) = 0, x = \underline{\hspace{2cm}}$

d. $g(x) = 4, x = \underline{\hspace{2cm}}$

Need help? Visit www.rsgsupport.org

3.6 Curbside Rivalry

A Solidify Understanding Task



CC BY apasciuto
<https://flic.kr/p/8n5b6e>

Carlos and Clarita have a brilliant idea for how they will earn money this summer. Since the community in which they live includes many high schools, a couple of universities, and even some professional sports teams, it seems that everyone has a favorite team they like to cheer for. In Carlos' and Clarita's neighborhood these rivalries take on special meaning, since many of the neighbors support different teams. They have observed that their neighbors often display handmade posters and other items to make their support of their favorite team known. The twins believe they can get people in the neighborhood to buy into their new project: painting team logos on curbs or driveways.

For a small fee, Carlos and Clarita will paint the logo of a team on a neighbor's curb, next to their house number. For a larger fee, the twins will paint a mascot on the driveway. Carlos and Clarita have designed stencils to make the painting easier and they have priced the cost of supplies. They have also surveyed neighbors to get a sense of how many people in the community might be interested in purchasing their service. Here is what they have decided, based on their research.

- *A curbside logo will require 48 in^2 of paint*
- *A driveway mascot will require 16 ft^2 of paint*
- *Surveys show the twins can sell 100 driveway mascots at a cost of \$20, and they will sell 10 fewer mascots for each additional \$5 they charge*

1. If a curbside logo is designed in the shape of a square, what will its dimensions be?

A square logo will not fit nicely on a curb, so Carlos and Clarita are experimenting with different types of rectangles. They are using a software application that allows them to stretch or shrink their logo designs to fit different rectangular dimensions.

2. Carlos likes the look of the logo when the rectangle in which it fits is 8 inches longer than it is wide. What would the dimensions of the curbside logo need to be to fit in this type of rectangle? As part of your work, write a quadratic equation that represents these requirements.

3. Clarita prefers the look of the logo when the rectangle in which it fits is 13 inches longer than it is wide. What would the dimensions of the curbside logo need to be to fit in this type of rectangle? As part of your work, write a quadratic equation that represents these requirements.

Your quadratic equations on the previous two problems probably started out looking like this:
 $x(x + n) = 48$ where n represents the number of inches the rectangle is longer than it is wide. The expression on the left of the equation could be multiplied out to get an equation of the form $x^2 + nx = 48$. If we subtract 48 from both sides of this equation we get $x^2 + nx - 48 = 0$. In this form, the expression on the left looks more like the quadratic functions you have been working with in previous tasks, $y = x^2 + nx - 48$.

4. Consider Carlos' quadratic equation where $n = 8$, so $x^2 + 8x - 48 = 0$. How can we use our work with quadratic functions like $y = x^2 + 8x - 48$ to help us solve the quadratic equation $x^2 + 8x - 48 = 0$? Describe at least two different strategies you might use, and then carry them out. Your strategies should give you solutions to the equation as well as a solution to the question Carlos is trying to answer in #2.

5. Now consider Clarita's quadratic equation where $n = 13$, so $x^2 + 13x - 48 = 0$. Describe at least two different strategies you might use to solve this equation, and then carry them out. Your strategies should give you solutions to the equation as well as a solution to the question Clarita is trying to answer in #3.

6. After much disagreement, Carlos and Clarita agree to design the curbside logo to fit in a rectangle that is 6 inches longer than it is wide. What would the dimensions of the curbside logo need to be to fit in this type of rectangle? As part of your work, write and solve a quadratic equation that represents these requirements.

9. Make a table, sketch a graph, and write an equation for the number of driveway mascots the twins can sell for each \$5 increment, x , in the price of the mascot.

number of \$5 increments in the price	number of mascots purchased
0	100
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

10. Make a table, sketch a graph (on the same set of axes), and write an equation for the price of a driveway mascot for each \$5 increment, x , in the price.

number of \$5 increments in the price	price of a mascot
0	20
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

11. Make a table, sketch a graph, and write an equation for the revenue the twins will collect for each \$5 increment in the price of the mascot.

number of \$5 increments in the price	Revenue = price \times number of mascots sold
0	2000
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

12. The twins estimate that the cost of supplies will be \$250 and they would like to make \$2000 in profit from selling driveway mascots. Therefore, they will need to collect \$2250 in revenue. Write and solve a quadratic equation that represents collecting \$2250 in revenue. Be sure to clearly show your strategy for solving this quadratic equation.

READY, SET, GO!

Name

Period

Date

READY

Topic: Finding x-intercepts for linear equations

1. Find the x-intercept of each equation below. Write your answer as an ordered pair. Consider how the format of the given equation either facilitates or inhibits your work.

a. $3x + 4y = 12$	b. $y = 5x - 3$	c. $y - 5 = -4(x + 1)$
d. $y = -4x + 1$	e. $y - 6 = 2(x + 7)$	f. $5x - 2y = 10$

2. Which of the linear equation formats above facilitates your work in finding x-intercepts? Why?

3. Using the same equations from question 1, find the y-intercepts. Write your answers as ordered pairs

a. $3x + 4y = 12$

b. $y = 5x - 3$

c. $y - 5 = -4(x + 1)$

d. $y = -4x + 1$

e. $y - 6 = 2(x + 7)$

f. $5x - 2y = 10$

4. Which of the formats above facilitate finding the y-intercept? Why?

Need help? Visit www.rsgsupport.org

SET

Topic: Solve Quadratic Equations, Connecting Quadratics with Area

For each of the given quadratic equations, (a) describe the rectangle the equation fits with. (b)

What constraints have been placed on the dimensions of the rectangle?

5. $x^2 + 7x - 170 = 0$

6. $x^2 + 15x - 16 = 0$

7. $x^2 + 2x - 35 = 0$

8. $x^2 + 10x - 80 = 0$

Solve the quadratic equations below.

9. $x^2 + 7x - 170 = 0$

10. $x^2 + 15x - 16 = 0$

11. $x^2 + 2x - 35 = 0$

12. $x^2 + 10x - 80 = 0$

GO

Topic: Factoring Expressions

Write each of the expressions below in factored form.

13. $x^2 - x - 132$

14. $x^2 - 5x - 36$

15. $x^2 + 5x + 6$

16. $x^2 + 13x + 42$

17. $x^2 + x - 56$

18. $x^2 - x$

19. $x^2 - 8x + 12$

20. $x^2 - 10x + 25$

21. $x^2 + 5x$

Need help? Visit www.rsgsupport.org

3.7 Perfecting My Quads

A Practice Understanding Task



CC BY William Warby
<https://flic.kr/p/8ur4Pb>

Carlos and Clarita, Tia and Tehani, and their best friend Zac are all discussing their favorite methods for solving quadratic equations of the form $ax^2 + bx + c = 0$. Each student thinks about the related quadratic function $y = ax^2 + bx + c$ as part of his or her strategy.

Carlos: “I like to make a table of values for x and find the solutions by inspecting the table.”

Zac: “I like to graph the related quadratic function and use my graph to find the solutions.”

Clarita: “I like to write the equation in factored form, and then use the factors to find the solutions.”

Tia: “I like to treat it like a quadratic function that I put in vertex form by completing the square. I can then use a square root to undo the squared expression.”

Tehani: “I also like to use the quadratic formula to find the solutions.”

Demonstrate how each student might solve each of the following quadratic equations.

Solve: $x^2 - 2x - 15 = 0$	<u>Carlos’ Strategy</u>	<u>Zac’s Strategy</u>
<u>Clarita’s Strategy</u>	<u>Tia’s Strategy</u>	<u>Tehani’s Strategy</u>

<p>Solve:</p> $2x^2 + 3x + 1 = 0$	<p><u>Carlos' Strategy</u></p>	<p><u>Zac's Strategy</u></p>
<p><u>Clarita's Strategy</u></p>	<p><u>Tia's Strategy</u></p>	<p><u>Tehani's Strategy</u></p>

<p>Solve:</p> $x^2 + 4x - 8 = 0$	<p><u>Carlos' Strategy</u></p>	<p><u>Zac's Strategy</u></p>
<p><u>Clarita's Strategy</u></p>	<p><u>Tia's Strategy</u></p>	<p><u>Tehani's Strategy</u></p>

Describe why each strategy works.

As the students continue to try out their strategies, they notice that sometimes one strategy works better than another. Explain how you would decide when to use each strategy.

Here is an extra challenge. How might each student solve the following system of equations?

<p>Solve the system:</p> $y_1 = x^2 - 4x + 1$ $y_2 = x - 3$	<p><u>Carlos' Strategy</u></p>	<p><u>Zac's Strategy</u></p>
<p><u>Clarita's Strategy</u></p>	<p><u>Tia's Strategy</u></p>	<p><u>Tehani's Strategy</u></p>

READY, SET, GO!

Name

Period

Date

READY

Topic: Symmetry and Distance

The given functions provide the connection between possible areas, $A(x)$, that can be created by a rectangle for a given side length, x , and a set amount of perimeter. You could think of it as the different amounts of area you can close in with a given amount of fencing as long as you always create a rectangular enclosure.

1. $A(x) = x(10 - x)$

Find the following:

a. $A(3) =$ b. $A(4) =$

c. $A(6) =$ d. $A(x) = 0$

e. When is $A(x)$ at its maximum? Explain or show how you know.

2. $A(x) = x(50 - x)$

Find the following:

a. $A(10) =$ b. $A(20) =$

c. $A(30) =$ d. $A(x) = 0$

e. When is $A(x)$ at its maximum? Explain or show how you know.

3. $A(x) = x(75 - x)$

Find the following:

a. $A(20) =$ b. $A(35) =$

c. $A(40) =$ d. $A(x) = 0$

e. When is $A(x)$ at its maximum? Explain or show how you know.

4. $A(x) = x(48 - x)$

Find the following:

a. $A(10) =$ b. $A(20) =$

c. $A(28) =$ d. $A(x) = 0$

e. When is $A(x)$ at its maximum? Explain or show how you know.

Need help? Visit www.rsgsupport.org

SET

Topic: Solve Quadratic Equations Efficiently

For each of the given quadratic equations find the solutions using an efficient method. State the method you are using as well as the solutions. You must use at least three different methods.

5. $x^2 + 17x + 60 = 0$ 6. $x^2 + 16x + 39 = 0$ 7. $x^2 + 7x - 5 = 0$

8. $3x^2 + 14x - 5 = 0$ 9. $x^2 - 12x = -8$ 10. $x^2 + 6x = 7$

Summarize the process for solving a quadratic by the indicated strategy. Give examples along with written explanation, also indicate when it is best to use this strategy.

11. Completing the Square

12. Factoring

13. Quadratic Formula

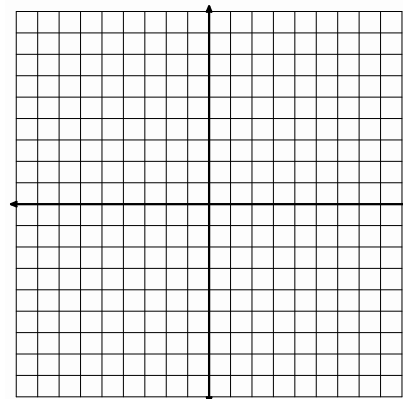
GO

Topic: Graphing Quadratics and finding essential features of the graph. Solving systems of equations.

Graph the quadratic function and supply the desired information about the graph.

14. $f(x) = x^2 + 8x + 13$

- a. Line of symmetry:
- b. x-intercepts:
- c. y-intercept:
- d. vertex:



Need help? Visit www.rsgsupport.org

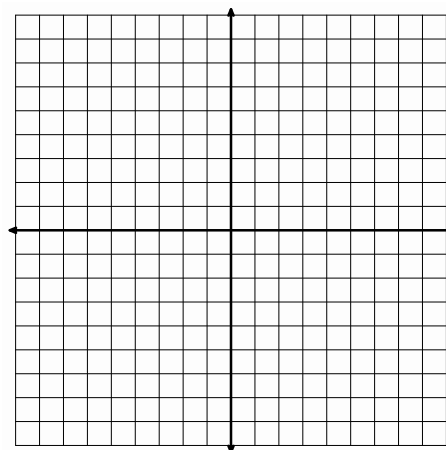
15. $f(x) = x^2 - 4x - 1$

a. Line of symmetry:

b. x-intercepts:

c. y-intercept:

d. vertex:



Solve each system of equations using an algebraic method and check your work!

16.

$$\begin{cases} 3x + 5y = 15 \\ 3x - 2y = 6 \end{cases}$$

17.

$$\begin{cases} y = -7x + 12 \\ y = 5x - 36 \end{cases}$$

18.

$$\begin{cases} y = 2x + 12 \\ y = 10x - x^2 \end{cases}$$

19.

$$\begin{cases} y = 24x - x^2 \\ y = 8x + 48 \end{cases}$$

Need help? Visit www.rsgsupport.org



CC BY Ben Salter
<https://flic.kr/p/5xVGij>

3.8 To Be Determined . . .

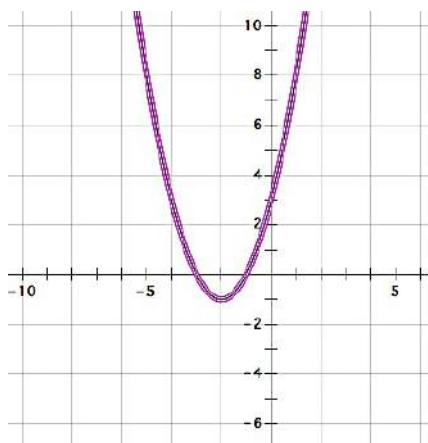
A Develop Understanding Task

Israel and Miriam are working together on a homework assignment. They need to write the equations of quadratic functions from the information given in a table or a graph. At first, this work seemed really easy. However, as they continued to work on the assignment, the algebra got more challenging and raised some interesting questions that they can't wait to ask their teacher.

Work through the following problems from Israel and Miriam's homework. Use the information in the table or the graph to write the equation of the quadratic function in all three forms. You may start with any form you choose, but you need to find all three equivalent forms. (If you get stuck, your teacher has some hints from Israel and Miriam that might help you.)

1.

x	y
-5	8
-4	3
-3	0
-2	-1
-1	0
0	3
1	8
2	15
3	24
4	35



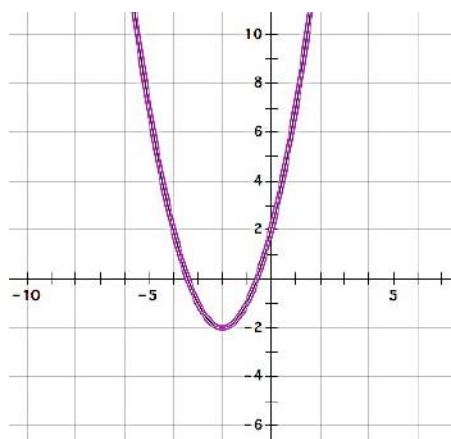
Standard form:

Factored form:

Vertex form:

2.

x	y
-5	7
-4	2
-3	-1
-2	-2
-1	-1
0	2
1	7
2	14
3	23
4	34



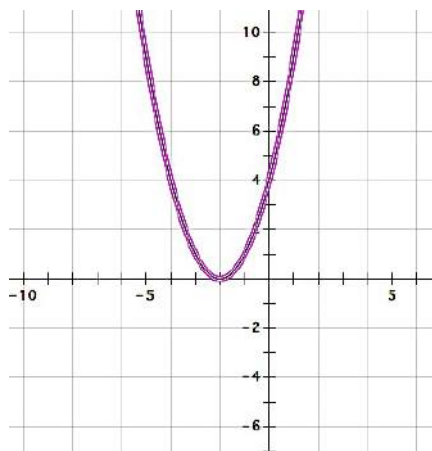
Standard form:

Factored form:

Vertex form:

3.

x	y
-5	9
-4	4
-3	1
-2	0
-1	1
0	4
1	9
2	16
3	25
4	36



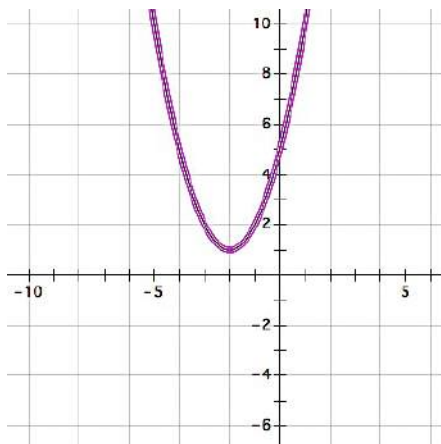
Standard form:

Factored form:

Vertex form:

4.

x	y
-5	10
-4	5
-3	2
-2	1
-1	2
0	5
1	10
2	17
3	26
4	37



Standard form:

Factored form:

Vertex form:

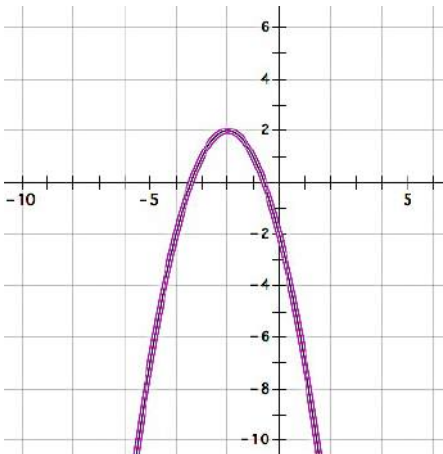
5. Israel was concerned that his factored form for the function in question 4 didn't look quite right. Miriam suggested that he test it out by plugging in some values for x to see if he gets the same points as those in the table. Test your factored form. Do you get the same values as those in the table?

6. Why might Israel be concerned about writing the factored form of the function in question 4?

Here are some more from Israel and Miriam's homework.

7.

x	y
-5	-7
-4	-2
-3	1
-2	2
-1	1
0	-2
1	-7
2	-14
3	-23
4	-34



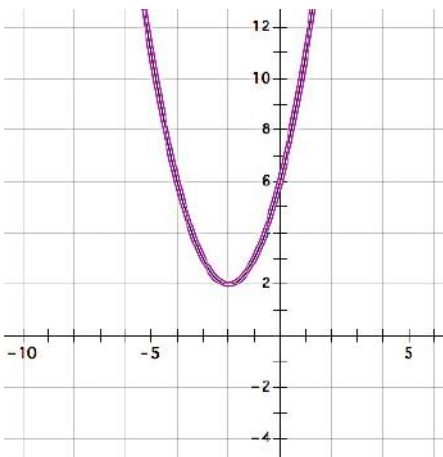
Standard form:

Factored form:

Vertex form:

8.

x	y
-5	11
-4	6
-3	3
-2	2
-1	3
0	6
1	11
2	18
3	27
4	38



Standard form:

Factored form:

Vertex form:

9. Miriam notices that the graphs of function 7 and function 8 have the same vertex point. Israel notices that the graphs of function 2 and function 7 are mirror images across the x -axis. What do you notice about the roots of these three quadratic functions?

The Fundamental Theorem of Algebra

A polynomial function is a function of the form:

$$y = a_0x^n + a_1x^{n-1} + a_2x^{n-2} + \cdots + a_{n-3}x^3 + a_{n-2}x^2 + a_{n-1}x + a_n$$

where all of the exponents are positive integers and all of the coefficients $a_0 \dots a_n$ are constants.

As the theory of finding roots of polynomial functions evolved, a 17th century mathematician, Girard (1595-1632) made the following claim which has come to be known as the Fundamental Theorem of Algebra: *An n^{th} degree polynomial function has n roots.*

10H. In later math classes you will study polynomial functions that contain higher-ordered terms such as x^3 or x^5 . Based on your work in this task, do you believe this theorem holds for quadratic functions? That is, do all functions of the form $y = ax^2 + bx + c$ always have two roots? [Examine the graphs of each of the quadratic functions you have written equations for in this task. Do they all have two roots? Why or why not?]

READY, SET, GO!	Name _____	Period _____	Date _____
-----------------	------------	--------------	------------

READY

Topic: Simplifying Radicals

Simplify each of the radicals below.

- | | | |
|----------------|----------------|----------------|
| 1. $\sqrt{8}$ | 2. $\sqrt{18}$ | 3. $\sqrt{32}$ |
| 4. $\sqrt{20}$ | 5. $\sqrt{45}$ | 6. $\sqrt{80}$ |

7. What is the connection between the radicals above? Explain.

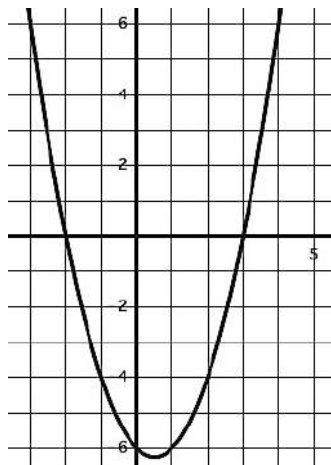
SET

Topic: Determine the nature of the x-intercepts for each quadratic below.

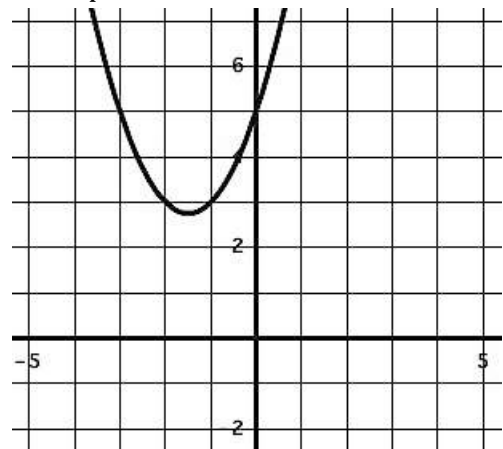
Given the quadratic function, its graph or other information, below determine the nature of the x-intercepts (what type of number it is). Explain or show how you know.

(Whole numbers “W”, Integers “Z”, Rational “Q”, Irrational “ \bar{Q} ”, or finally, “not Real”)

8. Determine the nature of the x-intercepts.



9. Determine the nature of the x-intercepts



Need help? Visit www.rsgsupport.org

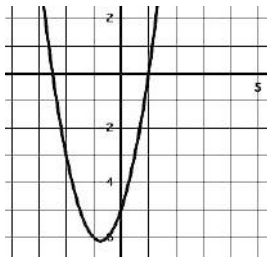
10. Determine the nature of the x-intercepts.

$$f(x) = x^2 + 4x - 24$$

11. Determine the nature of the x-intercepts.

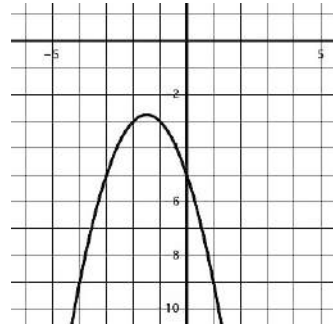
$$g(x) = (2x - 1)(5x + 2)$$

12. Determine the nature of the x-intercepts.



$$f(x) = 2x^2 + 3x - 5$$

13. Determine the nature of the x-intercepts.



14. Determine the nature of the x-intercepts.

$$r(t) = t^2 - 8t + 16$$

15. Determine the nature of the x-intercepts.

$$h(x) = 3x^2 - 5x + 9$$

Determine the number of roots that each polynomial will have.

16. $x^5 + 7x^3 - x^2 + 4x - 21$ 17. $4x^3 + 2x^2 - 3x - 9$ 18. $2x^7 + 4x^5 - 5x^2 + 16x + 3$

GO

Topic: Finding x-intercepts for quadratics using factoring and quadratic formula.

If the given quadratic function can be factored then factor and provide the x-intercepts. If you cannot factor the function then use the quadratic formula to find the x-intercepts.

19. $A(x) = x^2 + 4x - 21$ 20. $B(x) = 5x^2 + 16x + 3$ 21. $C(x) = x^2 - 4x + 1$

22. $D(x) = x^2 - 16x + 4$ 23. $E(x) = x^2 + 3x - 40$ 24. $F(x) = 2x^2 - 3x - 9$

25. $G(x) = x^2 - 3x$ 26. $H(x) = x^2 + 6x + 8$ 27. $K(x) = 3x^2 - 11$

Need help? Visit www.rsgsupport.org

3.9 My Irrational and Imaginary Friends

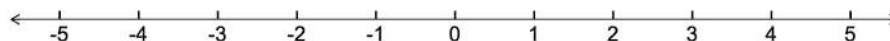
A Solidify Understanding Task



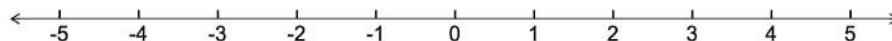
CC BY Funk Dooby
<https://flic.kr/p/f7YDU9>

Part 1: Irrational numbers

1. Verify that $4(x - \frac{5}{2})(x + \frac{3}{2}) = 0$ and $4x^2 - 4x - 15 = 0$ are equivalent equations (show your work), and plot the solutions to the quadratic equations on the following number line:

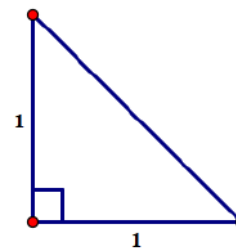


2. Verify that $(x - 2 + \sqrt{2})(x - 2 - \sqrt{2}) = 0$ and $4x^2 - 4x + 2 = 0$ are equivalent equations (show your work), and plot the solutions to the quadratic equations on the following number line:



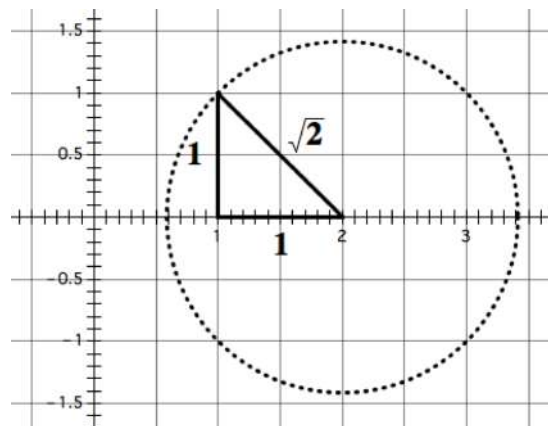
You may have found it difficult to locate the exact points on the number line that represent the two solutions to the 2nd pair of quadratic equations given above. The following diagrams might help.

3. Find the perimeter of this isosceles triangle. Express your answer as simply as possible.



We might approximate the perimeter of this triangle with a decimal number, but the exact perimeter is $2 + \sqrt{2}$, which cannot be simplified any farther. Note that this notation represents a single number—the distance around the perimeter of the triangle—even though it is written as the sum of two terms.

4. Explain how you could use this diagram to locate the two solutions to the quadratic equations given in the 2nd problem above: $2 + \sqrt{2}$ and $2 - \sqrt{2}$.



5. Are the numbers we have located on the number line in this way rational numbers or irrational numbers? Explain your answer.

Both sets of quadratic equations given in problems 1 and 2 above have solutions that can be plotted on a number line. The solutions to the first set of quadratic equations are rational numbers. The solutions to the 2nd set of quadratic equations are irrational numbers.

Big Idea #1: The set of numbers that contains all of the *rational numbers* and all of the *irrational numbers* is called the set of *real numbers*. The location of all points on a number line can be represented by real numbers.

Part 2: Imaginary and Complex Numbers

In the previous task, *To Be Determined . . .*, you found that the quadratic formula gives the solutions to the quadratic equation $x^2 + 4x + 5 = 0$ as $-2 + \sqrt{-1}$ and $-2 - \sqrt{-1}$. Because the square root of a negative number has no defined value as either a rational or an irrational number, Euler proposed that a new number $i = \sqrt{-1}$ be including in what came to be known as the complex number system.

6. Based on Euler's definition of i , what would the value of i^2 be?

With the introduction of the number i , the square root of *any* negative number can be represented.

For example, $\sqrt{-2} = \sqrt{2} \cdot \sqrt{-1} = \sqrt{2} \cdot i$ and $\sqrt{-9} = \sqrt{9} \cdot \sqrt{-1} = 3i$.

7. Find the values of the following expressions. Show the details of your work.

(a) $\sqrt{-16}$

(b) $2\sqrt{-121}$

Using this new notation, the solutions to the equation $x^2 + 4x + 5 = 0$ can be written as $-2 + i$ and $-2 - i$, and the factored form of $x^2 + 4x + 5$ can be written as $(x + 2 - i)(x + 2 + i)$.

8H. Verify that $x^2 + 4x + 5$ and $(x + 2 - i)(x + 2 + i)$ are equivalent by expanding and simplifying the factored form. Show the details of your work.

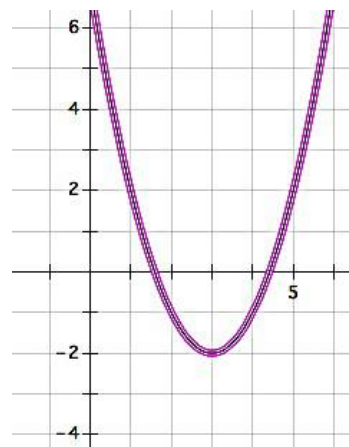
Big Idea #2: Numbers like $3i$ and $\sqrt{2} \cdot i$ are called *pure imaginary numbers*. Numbers like $-2 - i$ and $-2 + i$ that include a real term and an imaginary term are called *complex numbers*.

The quadratic formula is usually written in the form $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. An equivalent form is

$\frac{-b}{2a} \pm \frac{\sqrt{b^2 - 4ac}}{2a}$. If a , b and c are rational coefficients, then $\frac{-b}{2a}$ is a rational term, and $\frac{\sqrt{b^2 - 4ac}}{2a}$

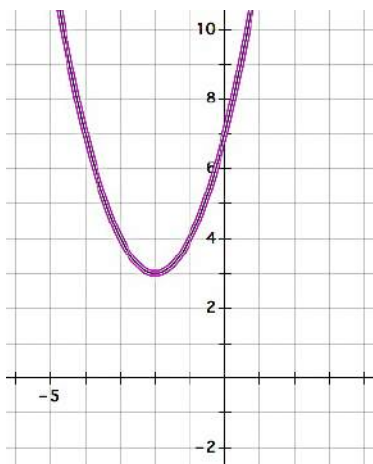
may be a rational term, an irrational term or an imaginary term, depending on the value of the expression under the square root sign.

9. Examine the roots of the quadratic $y = x^2 - 6x + 7$ shown in the graph at the right. How do the terms $\frac{-b}{2a}$ and $\frac{\sqrt{b^2 - 4ac}}{2a}$ show up in this graph?



Look back at the work you did in the task *To Be Determined* . . .

10. Which quadratics in that task had complex roots? (List them here.)
11. How can you determine if a quadratic has complex roots from its graph?
12. Find the complex roots of the following quadratic function represented by its graph.



13. Reflect the graph of the quadratic function given in question 12 over the horizontal line $y = 3$. Find the irrational roots of the reflected quadratic function.

14. How is the work you did to find the roots of the quadratic functions in questions 12 and 13 similar?

Big Idea #3: Complex numbers are not real numbers—they do not lie on the real number line that includes all of the rational and irrational numbers; also note that the real numbers are a subset of the complex numbers since a real number results when the imaginary part of $a + bi$ is 0, that is, $a + 0i$.

The Fundamental Theorem of Algebra, Revisited

Remember the following information given in the previous task:

A polynomial function is a function of the form:

$$y = a_0x^n + a_1x^{n-1} + a_2x^{n-2} + \cdots + a_{n-3}x^3 + a_{n-2}x^2 + a_{n-1}x + a_n$$

where all of the exponents are positive integers and all of the coefficients $a_0 \dots a_n$ are constants.

As the theory of finding roots of polynomial functions evolved, a 17th century mathematician, Girard (1595-1632) made the following claim which has come to be known as the Fundamental Theorem of Algebra: *An n^{th} degree polynomial function has n roots.*

15H. Based on your work in this task, do you believe this theorem holds for quadratic functions? That is, do all functions of the form $y = ax^2 + bx + c$ always have two roots? Explain your thinking.

READY, SET, GO!

Name

Period

Date

READY

Topic: Classifying numbers according to set.

Classify each of the numbers represented below according to the sets to which they belong. If a number fits in more than one set then list all that apply.

(Whole numbers "W", Integers "Z", Rational "Q", Irrational "Q̄", Real "R", Complex "C")

1. π

2. -13

3. $\sqrt{-16}$

4. 0

5. $\sqrt{75}$

6. $\frac{9}{3}$

7. $\sqrt{\frac{4}{9}}$

8. $5 + \sqrt{2}$

9. $\sqrt{-40}$

SET

Topic: Simplifying radicals, imaginary numbers

Simplify each radical expression below.

10. $3 + \sqrt{2} - 7 + 3\sqrt{2}$

11. $\sqrt{5} - 9 + 8\sqrt{5} + 11 - \sqrt{5}$

12. $\sqrt{12} + \sqrt{48}$

13. $\sqrt{8} - \sqrt{18} + \sqrt{32}$

14. $11\sqrt{7} - 5\sqrt{7}$

15. $7\sqrt{7} + 5\sqrt{3} - 3\sqrt{7} + \sqrt{3}$

Simplify. Express as a complex number using "i" if necessary.

16. $\sqrt{-2} \cdot \sqrt{-2}$

17. $7 + \sqrt{-25}$

18. $(4i)^2$

19. i^2

20. $(\sqrt{-4})^2$

21. $(2)(5i)^2$

Need help? Visit www.rsgsupport.org

Solve each quadratic equation over the set of complex numbers.

22. $x^2 + 100 = 0$

23. $t^2 + 24 = 0$

24. $x^2 - 6x + 13 = 0$

25. $r^2 - 2r + 5 = 0$

GO

Topic: Solve Quadratic Equations

Use the discriminant to determine the nature of the roots to the quadratic equation.

26. $x^2 - 5x + 7 = 0$

27. $x^2 - 5x + 6 = 0$

28. $2x^2 - 5x + 5 = 0$

29. $x^2 + 7x + 2 = 0$

30. $2x^2 + 7x + 6 = 0$

31. $2x^2 + 7x + 7 = 0$

32. $2x^2 - 7x + 6 = 0$

33. $2x^2 + 7x - 6 = 0$

34. $x^2 + 6x + 9 = 0$

Solve the quadratic equations below using an appropriate method.

35. $m^2 + 15m + 56 = 0$

36. $5x^2 - 3x + 7 = 0$

37. $x^2 - 10x + 21 = 0$

38. $6x^2 + 7x - 5 = 0$

Need help? Visit www.rsgsupport.org

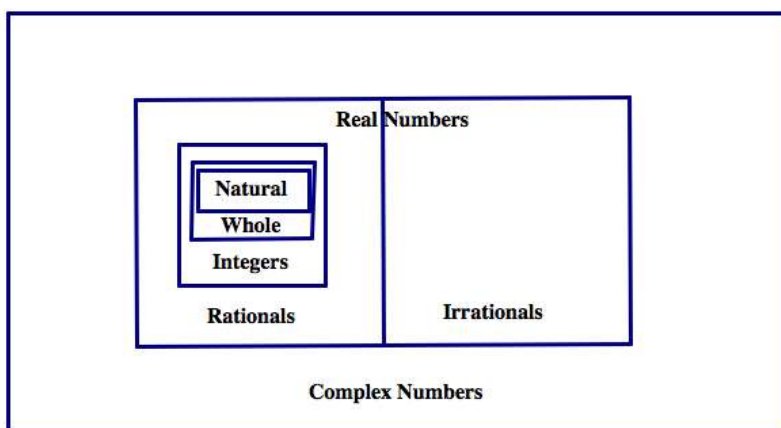
3.10 iNumbers

A Practice Understanding Task



CC BY Karlis Dambrans
<https://flic.kr/p/j1gEmS>

In order to find solutions to all quadratic equations, we have had to extend the number system to include complex numbers.



Do the following for each of the problems below:

- Choose the best word to complete each conjecture.
- After you have made a conjecture, create at least three examples to show why your conjecture is true.
- If you find a counter-example, change your conjecture to fit your work.

Conjecture #1: The sum of two integers is [always, sometimes, never] an integer.

Conjecture #2: The sum of two rational numbers is [always, sometimes, never] a rational number.

Conjecture #3: The sum of two irrational numbers is [always, sometimes, never] an irrational number.

Conjecture #4: The sum of two real numbers is [always, sometimes, never] a real number.

H: Conjecture #5: The sum of two complex numbers is [always, sometimes, never] a complex number.

Conjecture #6: The product of two integers is [always, sometimes, never] an integer.

Conjecture #7: The quotient of two integers is [always, sometimes, never] an integer.

Conjecture #8: The product of two rational numbers is [always, sometimes, never] a rational number.

Conjecture #9: The quotient of two rational numbers is [always, sometimes, never] a rational number.

Conjecture #10: The product of two irrational numbers is [always, sometimes, never] an irrational number.

Conjecture #11: The product of two real numbers is [always, sometimes, never] a real number.

H: Conjecture #12: The product of two complex numbers is [always, sometimes, never] a complex number.

13. The ratio of the circumference of a circle to its diameter is given by the irrational number π . Can the diameter of a circle and the circumference of the same circle both be rational numbers? Explain why or why not.

READY, SET, GO!

Name

Period

Date

READY

Topic: Attributes of quadratics and other functions

1. Summarize what you have learned about quadratic functions to this point. In addition to your written explanation provide graphs, tables and examples to illustrate what you know.

2. In prior work you have learned a great deal about both linear and exponential functions. Compare and contrast linear and exponential functions with quadratic functions. What similarities if any are there and what differences are there between linear, exponential and quadratic functions?

Need help? Visit www.rsgsupport.org

SET

Topic: Operations on different types of numbers

3. The Natural numbers, \mathbb{N} , are the numbers that come naturally or the counting numbers. As any child first learns numbers, they learn 1, 2, 3, ... What operations on the Natural numbers would cause the need for other types of numbers? What operation on Natural numbers create a need for Integers or Rational numbers and so forth. (Give examples and explain.)

In each of the problems below use the given items to determine whether or not it is possible *always, sometimes or never* to create a new element* that is in the desired set.

4. Using the operation of addition and elements from the Integers, \mathbb{Z} , [always, sometimes, never] an element of the Irrational numbers, $\bar{\mathbb{Q}}$, will be created. Explain.

5. Consider the equation $a - b = c$, where $a \in \mathbb{N}$ and $b \in \mathbb{N}$, c will be an Integer, \mathbb{Z} [always, sometimes, never]. Explain.

6. Consider the equation $a \div b = c$, where $a \in \mathbb{Z}$ and $b \in \mathbb{Z}$, then is $c \in \mathbb{Z}$ [sometimes, always, never]. Explain.

**The numbers in any given set of numbers may be referred to as elements of the set. For example, the Rational number set, \mathbb{Q} , contains elements or numbers that can be written in the form $\frac{a}{b}$, where a and b are integer values ($b \neq 0$).*

Need help? Visit www.rsgsupport.org

7. Using the operation of subtraction and elements from the Irrationals, $\overline{\mathbb{Q}}$, an element of the Irrational numbers, $\overline{\mathbb{Q}}$, will be created [always, sometimes, never]. Explain.

8. If two Complex numbers, \mathbb{C} , are subtracted the result will [always, sometimes, never] be a Complex number, \mathbb{C} . Explain.

GO

Topic: Solving all types of Quadratic Equations, Simplifying Radicals

Make a prediction as to the nature of the solutions for each quadratic (Real, Complex, Integer, etc.) then solve each of the quadratic equations below using an appropriate and efficient method. Give the solutions and compare to your prediction.

9. $-5x^2 + 3x + 2 = 0$

Prediction:

Solutions:

10. $x^2 + 3x + 2 = 0$

Prediction:

Solutions:

11. $x^2 + 3x - 12 = 0$

Prediction:

Solutions:

12. $4x^2 - 19x - 5 = 0$

Prediction:

Solutions:

Need help? Visit www.rsgsupport.org

Simplify each of the radical expressions. Use rational exponents if desired.

13. $\sqrt[4]{81x^8y^{12}}$

14. $\sqrt{\frac{a^7b^{10}}{a^3}}$

15. $\sqrt[5]{625x^{12}}$

16. $(\sqrt{n})^5$

17. $\sqrt[3]{-27}$

18. $(\sqrt{8})(\sqrt{3^2})(2)$

Fill in the table so each expression is written in radical form and with rational exponents.

	Radical Form	Exponential Form
19.	$\sqrt[4]{8^3}$	
20.		$256^{\frac{3}{4}}$
21.	$\sqrt[4]{2^7 \cdot 4^5}$	
22.		$16^{\frac{3}{2}} \cdot 4^{\frac{1}{2}}$
23.	$\sqrt[10]{x^{23}y^{31}}$	
24.	$\sqrt[5]{64a^9b^{18}}$	

Need help? Visit www.rsgsupport.org

4. What about this question: “How much should we charge if we want to maximize our revenue?”

As you probably observed, the situation represented in question 3 didn’t have a single solution, since there are many different prices the twins can charge to collect more than \$2250 in revenue. Sometimes our questions lead to quadratic inequalities rather than quadratic equations.

Here is another quadratic inequality based on your work on *Curbside Rivalry*.

5. Carlos and Clarita want to design a logo that requires less than 48 in² of paint, and fits inside a rectangle that is 8 inches longer than it is wide. What are the possible dimensions of the rectangular logo?

Again question 5 has multiple answers, and those answers are restricted by the context. Let’s examine the inequality you wrote for question 5, but not restricted by the context.

6. What are the solutions to the inequality $x(x + 8) < 48$?
7. How might you support your answer to question 6 with a graph or a table?

Here are some more quadratic inequalities without contexts. Show how you might use a graph, along with algebra, to solve each of them.

8. $x^2 + 3x - 10 \geq 0$

9. $2x^2 - 5x < 12$

10. $x^2 - 4 \leq 4x + 1$

Carlos and Clarita both used algebra and a graph to solve question 10, but they both did so in different ways. Illustrate each of their methods with a graph and with algebra.

11. Carlos: "I rewrote the inequality to get 0 on one side and a factored form on the other. I found the zeroes for each of my factors. To decide what values of x made sense in the inequality I also sketched a graph of the quadratic function that was related to the quadratic expression in my inequality. I shaded solutions for x based on the information from my graph."

12. Clarita: "I graphed a linear function and a quadratic function related to the linear and quadratic expressions in the inequality. From the graph I could estimate the points of intersection, but to be more exact I solved the quadratic equation $x^2 - 4 = 4x + 1$ by writing an equivalent equation that had 0 on one side. Once I knew the x -values for the points of intersection in the graph, I could shade solutions for x that made the inequality true."

READY, SET, GO!

Name

Period

Date

READY

Topic: Factoring Polynomials

Factor each of the polynomials completely.

1.

$$x^2 + x - 12$$

2.

$$x^2 - 2x - 8$$

3.

$$x^2 + 5x - 14$$

4.

$$x^2 - x - 6$$

5.

$$x^2 + 6x + 9$$

6.

$$x^2 - 7x + 10$$

7.

$$2x^2 - 9x - 5$$

8.

$$3x^2 - 3x - 18$$

9.

$$2x^2 + 8x - 42$$

10. How is the factored form of a quadratic helpful when graphing the parabola?

SET

Topic: Solving Quadratic Inequalities

Solve each of the quadratic inequalities.

11.

$$x^2 + x - 12 > 0$$

12.

$$x^2 - 2x - 8 \leq 0$$

13.

$$x^2 + 5x - 14 \geq 0$$

14.

$$2x^2 - 9x - 5 \geq 0$$

15.

$$3x^2 - 3x - 18 < 0$$

16.

$$x^2 + 4x - 21 < 0$$

17.

$$x^2 - 4x \leq 0$$

18.

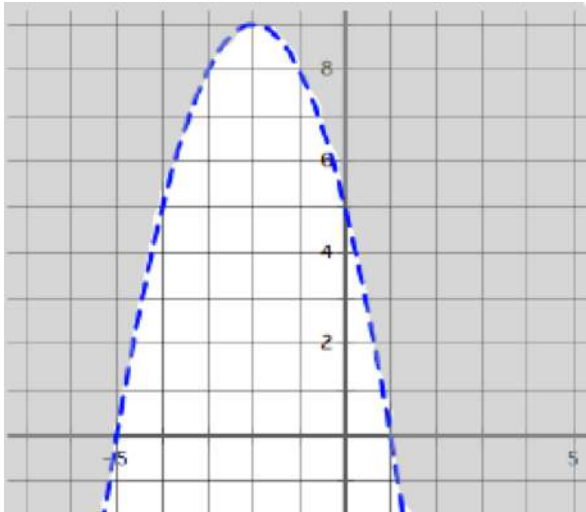
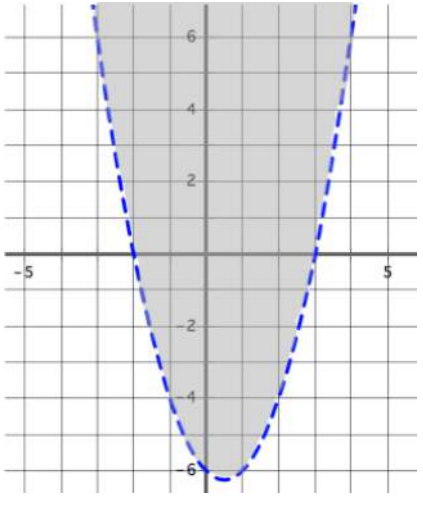
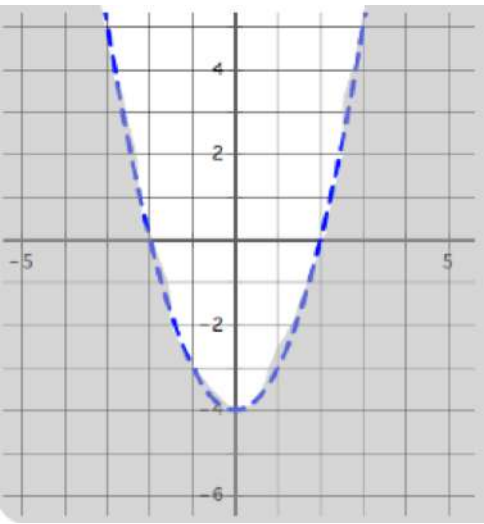
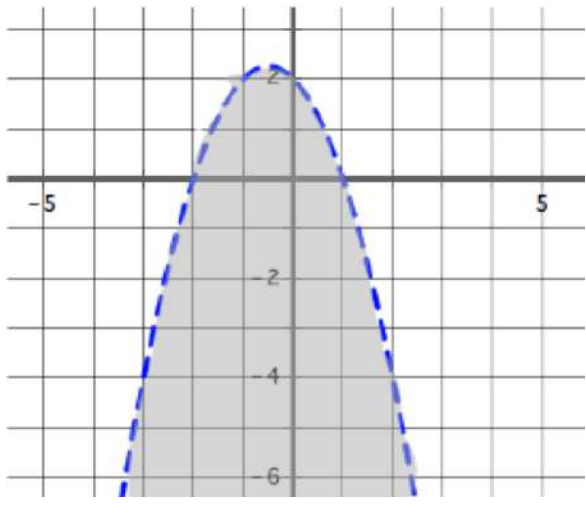
$$x^2 \leq 25$$

19.

$$x^2 - 4x \leq 5$$

Need help? Visit www.rsgsupport.org

Match each graph with its inequality.

<p>a.</p> 	<p>b.</p> 
<p>c.</p> 	<p>d.</p> 
<p>20. $y > x^2 - x - 6$</p>	<p>21. $y < x^2 - 4$</p>
<p>22. $y < (x + 2)(1 - x)$</p>	<p>23. $y > 5 - 4x - x^2$</p>

Need help? Visit www.rsgsupport.org

GO

Topic: Vertex form of quadratic equations

Write each quadratic function below in vertex form.

24.

$$f(x) = x^2 + 6x + 5$$

25.

$$f(x) = (x + 3)(x - 5)$$

26.

$$f(x) = (x - 2)(x + 6)$$

27.

$$f(x) = x^2 - 12x + 20$$

28.

$$f(x) = 2x^2 + 16x + 8$$

29.

$$f(x) = x^2 - 2x - 8$$

Need help? Visit www.rsgsupport.org